

Simple Machines

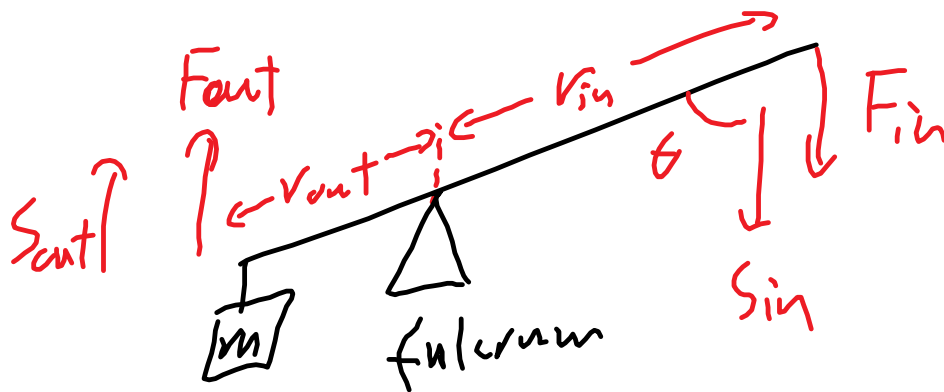
Lever, Wedge, pulleys, wheel and axel

Ideal Machine: efficiency is 100%

$$\text{efficiency} = W_{\text{out}}/W_{\text{in}} \times 100\%$$

so ideal Machine $W_{\text{out}} = W_{\text{in}}$

Look at a simple lever



Torque
 $\uparrow = F r \sin \theta$
 r is distance
from F to
rotation point

Ideal machine

$$W_{\text{out}} = W_{\text{in}}$$

$$F_{\text{out}} S_{\text{out}} = F_{\text{in}} S_{\text{in}}$$

$$\text{Mechanical Advantage, } MA = \frac{F_{\text{out}}}{F_{\text{in}}}$$

$$\rightarrow \text{Ideal Mechanical Advantage } IMA = \frac{F_{\text{out}}}{F_{\text{in}}} = \frac{S_{\text{in}}}{S_{\text{out}}}$$

eg. Your car has a flat tire. You want to jack up the tire 10cm. The mass of the car is 700kg, you only need to lift 1/4 to change one tire. Each push on the jack lifts the car 1.0 cm while your hand goes through 15 cm.

a) what is the weight of the car that you need to lift?

$$700 \times 9.81 / 4 = 1,716.75 \text{ N} \approx 1.7 \text{ kN}$$

b) what is the total distance your hand pushes through on the jack?

$$10 \times 15 \text{ cm} = 150 \text{ cm} = 1.5 \text{ m}$$

(you don't push on the way up)

c) What is the ideal mechanical advantage of the jack?

$$\text{IMA} = s_{\text{in}} / s_{\text{out}} = 150 \text{ cm} / 10 \text{ cm} = 15 \times$$

d) what is the minimum force you would have to apply on the jack?

$$F_{\text{in}} s_{\text{in}} = F_{\text{out}} s_{\text{out}}$$

$$F_{\text{in}} = (1,716.75 \times 0.1) / 1.5 = 114.45 \text{ N} \approx 1.1 \times 10^2 \text{ N}$$

$$\text{MA} = F_{\text{out}} / F_{\text{in}} \quad F_{\text{in}} = F_{\text{out}} / \text{MA} = 1,716.75 / 15 = 114.45$$

e) If you actually apply 150N on the jack, what is the mechanical advantage

$$\text{MA} = F_{\text{out}} / F_{\text{in}} = 1,716.75 / 150 = 11.445$$

11X

and efficiency of the jack?

efficiency = $W_{out}/W_{in} \times 100\%$

= $F_{out}s_{out}/F_{in}s_{in} \times 100\%$

= $(1,716.75 \times 0.1 / (150 \times 1.5)) \times 100 = 76.3$

76% efficiency

f) where did the lost energy go?

heat and sound due to friction

p206 -210

Q13, 15, 26, 37, 77, 86, 88